Nanoquasicrystalline Al-Fe-Cr-Ti alloy matrix/γ-Al2O3 nanocomposite powders: The effect of the ball milling process

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Abstract

Quasicrystalline aluminium alloys and aluminium based nanocomposites with the advantage of high strength over commercial aluminium alloys have been studied for many years. In this work a nanoquasicrystalline Al-Fe-Cr-Ti alloy powder and a nanocomposite consisting of a mixture of a nanoquasicrystalline alloy and nanosize γ -Al₂O₃ powders were produced through mechanical milling with different milling speeds. It has been observed that a higher milling time or milling speed can improve the homogeneity of the γ -Al₂O₃ distribution. The α-Al crystallite size decreases and the hardness increases with the milling time. The smallest crystallite size (14 nm) and the highest hardness value (638 HV_{10g}) were obtained for the nanocomposite after 30 hours of milling at 250 rpm. As the α-Al crystallite size is the main change in the microstructure during the ball milling process, the change in the hardness of the milled powders was found to follow a Hall-Petch type relation with an exponent of 0.25.

Key words: Mechanical milling, aluminium, quasicrystals, nanocomposites, hardness

1. Introduction

Compared with conventional alloys, composites have the advantages of high strength and high stiffness [\[1\]](#page-15-0). Decreasing the reinforcement particle size to nanoscale helps improving both the mechanical strength and the ductility. *Kang* et al. [\[2\]](#page-15-1) illustrated that $Al/1$ vol% Al_2O_3 (50nm) nanocomposite had almost the same tensile strength with the $Al/10$ vol% SiC (13 μ m) composite and much higher ductility. *Knowles* et al. [\[3\]](#page-15-2) processed Al6061/SiC nanocomposites through mechanical milling and hot isostatic pressing. With 12.9 vol% of SiC addition, the composites they processed increased the yield strength from 131 MPa to 229 MPa. The SiC has normally inert chemical behaviour with the matrix, but some authors reported that the SiC could react with Al, generating Al_4C_3 intermetallics and Al-Si eutectic, leading to undesired behaviour [\[4,](#page-15-3) [5\]](#page-15-4). Compared with the SiC, Al_2O_3 is widely used in aluminium based nanocomposites because it is chemically inert with Al [\[6\]](#page-15-5). Alumina is one of the most important structural materials with several transition phases that have enormous technological and industrial significance [\[7\]](#page-16-0). The γ-phase in particular is one of the polymorphic phases of alumina with numerous applications [\[7\]](#page-16-0). The γ -phase, with a cubic cell and a Fd-3m symmetry is a metastable phase and intrinsically nanocrystalline in nature that can also be easily synthesized by a variety of methods $[8, 9]$ $[8, 9]$. γ -Al₂O₃ can be transformed into the stable α -Al₂O₃ under heat treatment with a transformation sequence at high temperature (750°C-1200°C) [\[10\]](#page-16-3). The hardness of the γ-Al₂O₃ synthetized by different methods has been measured by several authors with values of 714 to 744 Kg/mm² [\[11-13\]](#page-16-4).

Mazaheri et al. [\[14\]](#page-16-5) fabricated an Al356/ α -Al₂O₃ composite through mechanical milling. The hardness they measured through nanoindentation increases from 75 kg/mm² to 216 kg/mm² with 20 vol.% of α -Al₂O₃ addition. This represents an increase in the hardness of 9.4% per % of the α -Al₂O₂ reinforcement, which is higher than the increase of 7.5% per % of SiC reinforcement obtained by *Knowles* et al [\[3\]](#page-15-2). Therefore, the use of nanosize γ -Al₂O₂ as reinforcement in Al-based composites is very promising is the nanoparticles' clusters can be broken-up and the nanoparticles are homogenously distributed in the Al alloy matrix.

Nanostructured Al-based alloys with a microstructure composed of nanoquasicrystalline particles embedded in an Al matrix, are well studied and known in the literature as "nanoquasicrystalline Al alloys" [\[15-22\]](#page-16-6). These alloys are normally produced by rapid solidification (melt-spinning or gas atomization) containing icosahedral quasicrystalline particles with typically size under 500 nm. *Inoue* et al. [\[18\]](#page-16-7) found ~45 vol.% of icosahedral particles for the Al93Fe3Cr2Ti2 (at.%) alloy atomized powder, and *Audebert* et al. [\[19\]](#page-16-8) found \sim 42 vol.% of icosahedral particles for the melt-spun Al₉₃Fe₃Cr₂Ti₂ (at.%) alloy. Nanoquasicrystalline Al alloys are attractive potential structural materials due to their high strength, particularly at elevated temperatures [\[19,](#page-16-8) [23\]](#page-17-0). These alloys can be used as metallic matrix of very high strength Al-based composites. In an early work *Galano* et al. [\[24\]](#page-17-1) milled a nanoquasicrystalline Al-based alloy powder with 8.5 vol.% of $γ$ -Al₂O₃ nanoparticles. Homogeneous alumina distribution on a nanoquasicrystalline matrix nanocomposite with high hardness value and minor quasicrystalline phase decomposition was obtained. In this work the ball milling process and the effects of processing parameters are investigated to produce a nanocomposite consisting of 12.9 vol.% γ -Al₂O₃ (20-50nm) distributed in a nanoquasicrystalline Al-Fe-Cr-Ti matrix. The effects of milling speed on the nano-size γ Al_2O_3 particles distribution in a nanoquasicrystalline Al-based matrix, the microstructure evolution and the hardness were investigated.

2. Experimental Methods

10 grams of gas atomized powder of the $Alg_3Fe_3Cr_2Ti_2$ (at%) nanoquasicrystalline alloy (A) with 25-50 µm powder size range and 12.9 vol.% γ -Al₂O₃ powder with particle size range of 20-50 nm were premixed in a Tubular mixer for 10 minutes. 100g stainless steel balls of 10 mm in diameter and the mixed powder were loaded into a 250 ml stainless steel vessel. This was done in an Argon filled glovebox. A Fritsch Mono Mill Pulverisette 6 Classic was used to process three batches of mixed powder with various milling speed from 200 rotates per minute (rpm) to 250 rpm. Twenty minutes pause was applied after each hour of milling to release the heat. For each powder batch, 0.5 grams was taken out after every 5 hours of milling until 30 hours. One batch of pure nanoquasicrystalline alloy powder was also milled with 250 rpm under the same milling conditions that the composite powders for comparison. The milling speed and the corresponding batch number are shown in Table 1. As shown, the milled powder samples are referred to as A*a*_*b* or C*a*_*b*, where A represents the nanoquasicrystalline alloy powder, and C the nanoquasicrystalline alloy plus alumina composites powders. The index *a* stands for the milling speed (rpm) and the index *b* for the milling hours, respectively.

X-ray diffractograms were obtained with a Bruker D5000 θ-2θ diffractometer with 0.15418 nm wavelength Cu-Kα radiation at 40 kV and 40 mA, with scan conditions of 2θ range of 20–100°, a step size of 0.02° and a scan rate of 0.003°/s. Crystallite sizes and the strain of ball milled powder were estimated by the Williamson-Hall plot method [\[25\]](#page-17-2). A FEI 200 focus ion beam (FIB) was used for milling the oxide layer away to observe the alumina distribution in the milled powders. The lift-out transmission electron microscope (TEM) samples with thickness ranging from 60-130 nm were prepared with the FIB apparatus. The crystallite sizes were measured on bright field TEM images taken in a Jeol 2100 TEM.

Vickers hardness (HV) was measured using a Wolpert hardness microindenter with 10 grams-force load and 15s of dwelling time. Powder samples were mounted in conductive Bakelite and polished until a metallographic quality surface. Vickers hardness was measured following the recommendations in the ASTM E384-16 standard [\[26\]](#page-17-3). Only powder particles with large circular surface in the mounted samples were measured with only one microindentation per powder particle. This allows meeting the recommended conditions of minimum thickness and the minimum distance from the centre of the indentation to the particle surface as 1.5 and 2.5 times of the indentation's diagonal, respectively. The Vickers hardness was calculated using the average value of the two diagonals of each microindentation and applying the corresponding formula for HV [\[26\]](#page-17-3) , as in equation (1):

$$
HV = 1854.4 \frac{P}{d^2}
$$
 (1)

Where, P is the load in gf; *d* is the average diagonal length value in μm. For each milled powder sample, 20 symmetric indentations were used to ensure the accuracy of the Vickers hardness values.

3. Results

3.1 Alumina distribution in the ball milled powder

The FIB images of the milled powder produced at 200 and 250 rpm are shown in Figure 1. For the C200 batch after 10 hours of milling (C200–10), the alumina appears in bands within the matrix, as shown in Figure 1 (a). Probably this is because the γ -Al₂O₃ particles that initially were stuck on the nanoquasicrystalline powder surface had been trapped inside when the quasicrystalline powder was cold welded together during the milling process. After 20 hours of milling (C200–20) the alumina distributes more homogeneously, as shown in Figure 1 (b). The progress towards to an alumina homogeneous distribution can be explained due to repeated cold-welding and fracturing cycles during the milling process [\[27\]](#page-17-4). The alumina distribution in the C250 batch powder follows a similar trend but more homogeneously than the C200 batch. In the C250_10 sample the alumina is distributed in the nanoquasicrystalline matrix forming thin bands with higher homogeneity than in the C200–10, (compare Figures 1 (a) and (c)). In the C250_20 sample the alumina seems quite homogeneously distributed (Figure 1 (d)) when compared with the C200_20 sample (Figure 1 (b)). The higher milling speed produces more collisions per unit volume of the powder leading to a more homogenous distribution for the same milling time.

Figure 1: FIB images of C200 and C250 milled powders with 10 and 20 hours milling time

3.2 Phases present in the ball milled powder

The X-ray diffractograms of the A250, C250 and C200 batches of powder are shown in Figure 2. Peaks at 2θ angles of 22.5, 40.9, 43.1, 73.1 degrees were indexed as corresponding to the icosahedral quasicrystalline phase using the Cahn's notation [\[28\]](#page-17-5). The peaks' intensity of the icosahedral quasicrystalline phase decreases with the milling time, which indicates a possible decomposition and/or a high distortion of the quasicrystalline phase structure by the ball collisions during the milling process. Only one small peak of the γ -Al₂O₃ was observed, the γ (440) peak, identified in the composite powders. This could be due to a combination of low volume fraction and the nano-size particles of the γ-Al₂O₃ in the nanocomposites powder, which produces broad and low intensity diffraction peaks, as it was observed in a previous work [\[24\]](#page-17-1). The quasicrystal and the α-Al peaks show broadenings with the milling time, which can be related with collisions and the fracturing process that reduce the Al crystallite size and distorts the Al and quasicrystal lattices.

Figure 2: The X-ray diffractograms of the milled powder samples

The icosahedral quasicrystalline phase and the γ -Al₂O₃ particles were also observed in the TEM analysis, as can be seen in the bright field TEM images from C200_10 and $C250/200$ 10 samples in Figure 3 (a) and (b), respectively. The particle (1) is an icosahedral quasicrystal phase characterised by the convergent beam electron diffraction patterns from the mirror zone axis. The particle (3) is an icosahedral quasicrystal according to the fivefold diffraction pattern with quasiperiodic order. The particles (2) and (4) would correspond to γ - Al_2O_3 particles according to the EDX analysis showed in the inset in Figure 3. Particle (4) has higher aluminium atom percentage, probably because the EDX detector received information from the aluminium matrix.

Figure 3: Bright field TEM image of the (a) C200_10 (b) C250/200_10 samples; with insets of electron diffraction patterns of icosahedral quasicrystalline particles (particles 1 and 3) and EDX results from alumina particles (particles 2 and 4).

3.3 The Al crystallite size, the strain and the hardness

The average Al crystallite size and the strain values of the ball milled powders were estimated through the Williamson-Hall plot method and summarised in Figure 4. Only powder samples of the C200 batch with milling time equal or higher than 20 hours, and samples of the C250/200 and C250 batches with milling time equal or higher than 10 hours were used for this estimation since Williamson-Hall plot produces large errors for Al crystallite sizes larger than 100 nm [\[24\]](#page-17-1). The Al crystallite sizes of the C250/200_5 and C250 5 samples were measured instead by drawing two pairs of parallel vertical and horizontal lines on each crystallite in the TEM images. The average distance between the vertical lines and the horizontal lines measured on at least 30 Al crystallites was taken as the average Al crystallite size.

The average Al crystallite size of the milled powder decreases with milling time and speed, as shown in Figure 4. For example, for the C200 batch the Al crystallite size decreases from 99 nm to 30 nm from 20 to 30 hours of milling. In the C250 batch the crystallite size decreases from 130 nm to 14 nm from 5 to 30 hours of milling. It is observed that for the same milling time, samples produced with higher milling speed have smaller average Al crystallite size.

The strain values of all milled powder batches do not show a clear trend. Most of the values lay between 1.0% and 1.5%.

The Vickers hardness of the milled powder is also shown in Figure 4. C200 batch samples with milling time lower than 20 hours had an inhomogeneous microstructure therefore Vickers hardness tests were not performed on these samples with very inhomogeneous microstructure. Before milling the Vickers hardness of the nanoquasicrystalline alloy powder was 132 ± 10 HV_{10g}. The hardness values of all the nanocomposite samples (C batches) increases with milling time and milling speed. The highest hardness values were observed for the C250 batch samples. These values increased from $407+59$ to $638+44$ HV_{10g} from 5 to 30 hours of milling. The C250 nanocomposite batch showed higher hardness values than the A250 nanoquasicrystalline alloy batch.

Figure 4: The Al crystallite size, the Al crystallite strain and the Vickers hardness values of the ball milled powders against the milling time.

4. Discussion

The hardness value (HV_{40}) measured on the unmilled nanoquasicrystalline alloy powder includes the contribution of all the strengthening mechanisms related to the nanoquasicrystalline alloy microstructure features. Considering that the volume fraction and the nano-size of quasicrystal/intermetallic precipitates embedded in the Al phase matrix (nanoquasicrystalline Al alloy) do not change during the ball milling process, the strengthening contribution by the Orowan's mechanism will remain constant with the milling time. In high strength alloys in which the particle and grain boundaries mechanisms are the main strengthening mechanisms, the solid solution represents a minor fraction contribution $(\leq 5\%)$ and the change in hardness during the milling process due to solid solution changes is even much lower [\[29,](#page-17-6) [30\]](#page-17-7). The dislocation-dislocation interaction strengthening mechanism is related with the dislocations density and therefore with the strain [\[31\]](#page-17-8). Figure 4 shows strain is lower than 1.5% and does not follow a clear trend, which suggests this strengthening mechanism does not contribute further to the hardness change with the milling time. From Figure 4 it is also observed that the Al crystallite size strongly decreases while the Vickers hardness increases with the milling time. Finally, it is reasonable to consider that the "change" in hardness values with the milling time is related mainly to the Al crystallite size refining. This suggests that the "increasing" of the materials strength should be related to the grain boundaries strengthening mechanism [\[32,](#page-17-9) [33\]](#page-18-0).

The main hardening contributions to the nanoquasicrystalline alloy are the related to the Orowan's mechanism due to the ~45 vol.% of quasicrystals/intermetallic nano-size particles and to the grain boundaries (Hall-Petch) mechanism with an Al grain size of $d_0 \sim 1 \mu m$ [\[19,](#page-16-8) [23\]](#page-17-0). Then, during the ball milling process, when the Al crystallites are heavily refined, the "change" of the hardness of the nanoquasicrystalline alloy (A250) will follow a Hall-Petch type relationship as a function of the Al crystallite size. A general expression of hardening as a consequence of the crystallite refining is normally written as:

$$
H = H_0 + \frac{k}{d^p} \qquad \qquad \text{---} \qquad \text{Equation (2)}
$$

Where *H* is the hardening due to the crystallite size (d) , H_0 is the lattice frictional stress, *k* is a constant known as "locking parameter", which measures the relative hardening contribution of the grain boundaries [\[34\]](#page-18-1), and *p* is a constant exponent. This exponent was suggested as *p* = 0.5 by the early works of *Hall* [\[32\]](#page-17-9) and *Petch* [\[33\]](#page-18-0). Deviations of this value have been theoretically proposed and experimentally found in the literature. Very early works by *Mathewson* in 1919 and *Bragg* in 1942 postulate that strength due to the crystallite size is proportional to $d^{0.25}$ and d^1 , respectively [\[35,](#page-18-2) [36\]](#page-18-3). Theoretical estimations in the literature for the *p* value also suggested values as: 1.0, 0.5, 0.33, and 0.25. Each of these values for *p* is based on different mechanisms and/or models for dislocation-grain boundary interactions. For example, the more common value, $p = 0.5$, is normally related to dislocations pile up at the grain boundaries; and *p* = 0.25 was also found by *Conrad* considering a dislocation forest hardening concept [\[37,](#page-18-4) [38\]](#page-18-5). Several models considering different dislocation-grain boundaries interactions, crystallite size ranges, boundaries features as porosity and impurities, solute diffusivity, dislocation sources have been proposed leading to different *p* values and even different complex equations as a function of the crystallite size [\[39\]](#page-18-6). The ball milling process introduces several physical changes in the Al lattice and grain boundaries that make it extremely difficult to build up a theoretical approach to propose an equation that accurately describes the hardening mechanism related to the crystallite refining experimentally observed. Thus, the experimental results obtained from the milled alloy and composite powder were fitted following the simple equation (2), finding an exponent $p = 0.25$ for the best lineal correlation between measured H values and 1 $\frac{1}{d^p}$, as can be seen in Figure 5 for the

alloy powder (a) and the composite powder (b). The lineal correlation following a Hall-Petch type relationship suggests that during the milling process of the alloy and the composite the hardening is mainly controlled by the crystallite refining, as was deduced above. Therefore, it is reasonable to suggest that the "change" of hardness respect to the initial hardness of the unmilled powder can be represented by $\frac{k}{d^p}$. Finally, the hardness value of the milled alloy powder after x hours of milling, H_{Ax} , can be estimated using equation (3):

$$
H_{Ax} = (H_{A0} - \frac{kA}{d_0^4}) + \frac{kA}{d_x^4} \qquad \qquad \text{---} \qquad \qquad \text{Equation (3)}
$$

Where k_A is the "locking parameter" for the alloy, and H_{A0} is the microhardness value of the unmilled nanoquasicrystalline Al-Fe-Cr-Ti alloy powder (measured as 132 ± 10 HV_{10g}) that includes the Al lattice frictional stress, the effects of solutes in the Al solid solution, quasicrystal/intermetallic particles hardening, grain boundaries hardening and other minor contributions. Thus, in order to count only the constant hardening contributions of the microstructure of the milled powders, the grain boundaries contribution for the initial Al

grain size (d_0) must be subtracted as: kA d_0^4 1 4 from H_{A0} . d_x is the Al crystallite size after x hours of

milling, which is the main observed microstructural feature that changes during the ball milling process in the nanoquasicrystalline alloy powder. For the unmilled alloy powder, when $d_x = d_0$ the equation (3) provides a hardness value equal to the measured hardness of the unmilled alloy powder, H_{A0} .

For the composite powders, because of the addition of the nano γ -Al₂O₃ particles, other strengthening contributions must be considered. Numerous theoretical models have been developed to correlate the mechanical behaviour of metal matrix composites with their microstructural characteristics [40-46]. These models might be grouped into three general categories: (1) load transfer models, (2) matrix strengthening models and (3) hybrid models.

(1): the load transfer models were developed on the basis that the hard, relatively undeformable reinforcements, may carry more load than the relatively soft matrix [\[40-42\]](#page-18-7). In this group is included the simplest and well know rule of mixtures (ROM) [\[42\]](#page-18-8), which is characterized for a mathematical expression which gives the homogeneous property of a heterogeneous materials in terms of the properties, quantity and arrangement of its constituents. This model weights the volume average of the component properties in isolation without considering any interaction between reinforcement and matrix. See equation (4) as applicable for the composite's hardness:

 = (1 −) + ------------- Equation (4)

where H_c , H_A , H_r are the hardness values for the composite, the matrix alloy and the reinforcement, respectively. f is the volume fraction of reinforcements.

(2): In the matrix strengthening models, the strengthening effect has been attributed to various microstructural changes experienced by the matrix as a result of the presence of reinforcement particulates [\[43\]](#page-18-9). For example, the stress increment resulting from the difference of the thermal expansion coefficient of matrix and reinforcement when the nanomaterial process involves temperature changes; an increase in strengthening by Orowan's mechanism when the reinforcements are located inside of the matrix grains.

(3): other authors proposed hybrid models that combine both approaches of load transfer and effects of the matrix microstructural changes due to the reinforcements addition [\[44-46\]](#page-18-10).

In the present work, we adopt a hybrid model to evaluate the hardness change with the ball milling time of a composite powder using the equation (5):

$$
H_{Cx} = \left[(H_{A0} - \frac{kc}{\frac{1}{d_0^4}}) + \frac{kc}{\frac{1}{d_x^4}} \right] (1 - f) + H_r f \quad \text{........} \quad \text{Equation (5)}
$$

where H_{Cx} is the hardness of the nanocomposite after x hours of milling, k_C is the "locking" parameter" for the composite, f is the volume fraction of the γ -Al₂O₃ reinforcement (12.9%), and H_r is the hardness value of the reinforcement (γ -Al₂O₃ with an average value taken from literature as 730 Kg/mm²) [\[11-13\]](#page-16-4). When no reinforcement is added to the powder alloy ($f =$ 0) equation (5) becomes equation (3) giving the hardness values for the milled alloy powders. The equation (5) predict a theoretical hardness value of the unmilled composite of $H_{C0} = 209$ $Kg/mm²$ by the application of the simple rule of mixtures.

It is worth mentioning that in composite systems where the reinforcement particle is much harder than the matrix or the volume fraction of the reinforcement is low, the ROM as in equation (4) may not predict the actual hardness of the composite due high plastic deformation around the hard particles that produce a zone of high dislocations density [\[42\]](#page-18-8). For example, for the $Ag-Al_2O_3$ composites, with a very soft Ag matrix, the experimental values of the hardness are almost the same up to 50 vol.% $A1_2O_3$ [\[47\]](#page-18-11). However, in the literature, for mechanical milled aluminium composites with about 10-20% volume fraction of ceramic reinforcement particles, the experimental results match the value estimated with the rule of mixtures [\[14,](#page-16-5) [48\]](#page-18-12). The equation (5) combines the equation (3) and the rule of mixtures (equation (4)). The mechanical milling and alumina affects the microstructure of the nanoquasicrystalline Al alloy matrix of the composite. As discussed above, the main observed microstructural features that change with the milling time in the composite are the refining of the Al crystallites in the matrix and a continue homogenisation of alumina distribution. The effect on the alloy matrix introduced by the γ -Al₂O₃ reinforcement is represented in the equation (5) by the term: $\frac{kc}{dP}$ d_x^P $\frac{c}{p}(1-f)$ were *f* considers the quantity of

reinforcement in the composite, d_x the size of the crystallite size in the matrix alloy, and the exponent $p = 0.25$, which in this work was obtained by fitting the hardness and Al crystallite size measured on the milled powders. This *p* value matches with the early model proposed by *Conrad and Hirth* [\[37,](#page-18-4) [38\]](#page-18-5) that consider a dislocation forest hardening concept. Moreover, the parameter k_C that was fitted for the composite powder is different than the one for the alloy powder (k_A) . The "blocking parameter", k , is associated with the stress required to extend dislocations activity into nearby grains and is very sensitive to the composition of the alloy and composites [\[34,](#page-18-1) [50-53\]](#page-19-0). For example, when adding 4 wt.% of Cu to the pure Al, the k value resulted more than 2 times of the one corresponding to the nanocrystalline pure Al [\[50,](#page-19-0) [51\]](#page-19-1). In the present work, considering that some γ -Al₂O₃ nanoparticles would be distributed at the Al grain boundaries in the alloy matrix, the hardening behaviour in the alloy and in the composite powders would be different, which lead to different *k* values that measures the properties of the grain boundaries as a sink and source of dislocations [\[49\]](#page-19-2).

In Figure 5 (a) the slope of the linear fitting for the milled alloy powder resulted as k_A = 1463±183 *kg*/mm² ⋅ nm^{1/4} (2551± 319 MPa ⋅ μm^{1/4}). The k_C value for the milled composite powders was also fitted linearly as can be observed in Figure 5 (b) taken the data for all the composite powder batches, finding a value of the slope as: $k_c(1 - f) = 938 \pm 122$ $kg/mm^2 \cdot nm^{1/4}$. Thus, $k_c = 1077 \pm 140 kg/mm^2 \cdot nm^{1/4}$ (1878 \pm 244 MPa $\cdot \mu m^{1/4}$), which is lower than the obtained for the milled alloy powders showing the effect of the γ -Al₂O₃ nanoparticles on the Al grain boundaries of the alloy matrix.

The values estimated from the linear fitting for the alloy data have larger errors, probably due to the limited number of samples in comparison with the data obtained for the composite powders. The data for the alloy and the composite were statistically evaluated by means of the Chauvenet's criterion [\[54\]](#page-19-3) and only one data for the alloy has not been taken into account in the fitting; the one corresponded to the A250_15 sample (crossed in Figure 5 (a)).

 (b)

Figure 5: The linear fit model for the (a) milled alloy and (b) nanocomposite powders. The measured Vickers hardness against d-0.25 (d: Al crystallite size)

The application of the equations (3) and (5) to predict the hardness value of the milled nanoquasicrystalline Al-Fe-Cr-Ti alloy and for it composites containing 12.9 vol.% γ-Al₂O₃ (20-50 nm) powders provided hardness values slightly lower but inside the error of the measured hardness values. The estimated hardness powders milled for 30 hs present higher deviation $(-15%)$, which can be explained because after 30 hs of milling some icosahedral quasicrystalline particles appear to be transformed which change the alloy matrix and as consequence the microstructural parameters in the equations should change too.

The hardness value obtained for the nanoquasicrystalline Al-Fe-Cr-Ti alloy matrix/ γ -Al₂O₃ particles nanocomposite powders are very high in comparison with the ones found in the literature, which are summarised in Table 2. This can be explained because of the large volume fraction $(-42-45%)$ of the quasicrystal nanoparticles embedded in fcc-Al phase, obtained by rapid solidification, produces a high strength alloy which can transfer load to the hard γ -Al₂O₃ reinforcements more efficiently than softer Al-based commercial alloys.

Table 2: The Al crystallite size and hardness values of ball milled composite powders in literature. NQX is the abbreviation of the nanoquasicrystalline Al alloy

5. Conclusion

The nanoquasicrystalline $\text{Al}_{93}\text{Fe}_{3}\text{Cr}_{2}\text{Ti}_{2}$ alloy based nanocomposites powder containing 12.9 vol.% γ-Al₂O₃ (20-50nm) has been produced by mechanical milling process. Homogeneous γ -Al₂O₃ distribution and very high Vickers hardness is obtained after 20 hours of milling at 200 rpm or for 10 hours of milling at 250 rpm. The metastable quasicrystalline phase has remained after 30 hours of milling even at 250 rpm.

As the milling speed increases, collisions per unit volume of the powder increase; thus distributes the alumina particles, refines the Al crystallite size and increases the hardness of the composites more efficiently.

The hardness of the nanoquasicrystalline Al alloy powder is mainly controlled by the refining of the Al crystallite size during the milling process. Thus the hardness change of the milled nanoquasicrystalline Al alloy powder can be estimated by a simple Hall-Petch type relationship with an exponent of 0.25 in accordance of early models based on dislocation forest hardening concept.

The hardness change of the ball milled nanocomposite powder can be estimated by a hybrid model that combines a Hall-Petch type relationship with an exponent of 0.25 and the rule of mixtures.

The addition of 12.9 vol.% γ-Al₂O₃ (20-50nm) particles to the nanoquasicrystalline $Alg₃Fe₃Cr₂Ti₂$ alloy powder processed by ball milling with a ball to powder ratio of 10, at 250 rpm during 30 hs allows to obtain an homogeneous nanocomposite powder with 4.8 times higher hardness (HV_{10g} = 638) than that of the nanoquasicrystalline Al alloy matrix (HV_{10g} = 132).

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